

Section 2 - Factoring by GCF

Factor each polynomial. Check your answer.

1. $8c^2 + 7c$

$c(8c + 7)$

2. $3n^3 + 12n^2$

$3n^2(n + 4)$

3. $15x^5 - 18x$

$3x(5x^4 - 6)$

4. $-8s^4 + 20t^3 - 28$

$-4(2s^4 - 5t^3 + 7)$

5. $6n^5 + 18n^3 - 24n$

$6n(n^4 + 3n^2 - 4)$

6. $-5m^4 - 5m^3 + 5m^2$

$-5m^2(m^2 + m - 1)$

Factor each expression.

7. $3m(m + 5) + 4(m + 5)$

$(m + 5)(3m + 4)$

8. $16b(b - 3) + (b - 3)$

$(b - 3)(16b + 1)$

9. $10d^2 - 6d(35d - 21)$

$2d(5d - 3) + 7(5d - 3)$

$(5d - 3)(2d + 7)$

10. $(12n^3 - 15n^2)(-8n + 10)$

$3n^2(4n - 5) - 2(4n - 5)$

$(4n - 5)(3n^2 - 2)$

can not airplane
 $b = 0 \text{ dd ?}$

mult
 $(3)(-2) = -6$
 $-1, 6$
 $1, -6$
 $-2, 3$
 $2, -3$

Name _____

Date _____

Class _____

Section 3 - Factoring $x^2 + bx + c$

Factor each trinomial.

1. $x^2 + 9x + 14$

Mult = 14
Add = 9

$(x + 7)(x + 2)$

2. $x^2 + 7x + 12$

M: 12
A: 7

$(x + 4)(x + 3)$

3. $x^2 + 9x + 18$

M: 18
A: 9

$(x + 3)(x + 6)$

4. $x^2 - 12x + 20$

M: 20
A: -12

$(x - 10)(x - 2)$

5. $x^2 - 11x + 18$

M: 18
A: -11

$(x - 9)(x - 2)$

6. $x^2 - 12x + 32$

M: 32
A: -12

$(x - 8)(x - 4)$

7. $x^2 + 2x - 15$

M: -15
A: 2

$(x + 5)(x - 3)$

8. $x^2 + 5x - 6$

M: -6
A: 5

$(x + 6)(x - 1)$

9. $x^2 + 5x - 24$

M: -24
A: 5

$(x + 8)(x - 3)$

10. $x^2 - x - 56$

M: -56
A: -1

$(x - 8)(x + 7)$

11. $x^2 - 2x - 8$

M: -8
A: -2

$(x - 4)(x + 2)$

12. $x^2 - x - 20$

M: -20
A: -1

$(x - 5)(x + 4)$

Section 4 - Factoring $ax^2 + bx + c$

Factor each trinomial.

1. $2x^2 + 13x + 15$ M: 30
A: 13

$$\left(\frac{2x+10}{2}\right)\left(\frac{2x+3}{2}\right)$$

$$\boxed{(x+5)(2x+3)}$$

2. $3x^2 + 10x + 8$ M: 24
A: 10

$$\left(\frac{3x+6}{3}\right)(3x+4)$$

$$\boxed{(x+2)(3x+4)}$$

3. $4x^2 + 24x + 27$ M: 108
A: 24

$$\left(\frac{4x+18}{2}\right)\left(\frac{4x+6}{2}\right)$$

$$\boxed{(2x+9)(2x+3)}$$

4. $7x^2 - 59x + 24$ M: 168
A: -59

$$(7x-3)\left(\frac{7x-56}{7}\right)$$

$$\boxed{(7x-3)(x-8)}$$

5. $3x^2 - 14x + 15$ M: 45
A: -14

$$\left(\frac{3x-9}{3}\right)(3x-5)$$

$$\boxed{(x-3)(3x-5)}$$

6. $8x^2 - 73x + 9$ M: 72
A: -73

$$\left(\frac{8x-72}{8}\right)(8x-1)$$

$$\boxed{(x-9)(8x-1)}$$

7. $8x^2 + 29x - 12$ M: -96
A: 29

$$\left(\frac{8x+32}{8}\right)(8x-3)$$

$$\boxed{(x+4)(8x-3)}$$

8. $11x^2 + 25x - 24$ M: -264
A: 25

$$\left(\frac{11x+33}{11}\right)(11x-8)$$

$$\boxed{(x+3)(11x-8)}$$

9. $9x^2 - 3x - 2$ M: -18
A: -3

$$\left(\frac{9x-6}{3}\right)\left(\frac{9x+3}{3}\right)$$

$$\boxed{(3x-2)(3x+1)}$$

10. The area of a rectangle is $20x^2 - 27x - 8$. The length is $4x + 1$. What is the width?

mult.
mult.

$$\begin{array}{c} \text{F} \qquad \qquad \text{L} \\ \underbrace{(4x+1)}_{\text{F}} \underbrace{(5x-8)}_{\text{L}} \\ 20x^2 - 8 \end{array}$$

$$\boxed{(5x-8)}$$

check: 0 I

$$-32x + 5x = -27x$$

Section 5 - Factoring Special Products

Factor each polynomial.

1. $x^2 + 6x + 9$

M: 9
A: 6

$(x+3)(x+3)$

2. $9x^2 - 12x + 4$

M: $3b$
A: -12

$(9x-6)(9x-6)$

$(3x-2)(3x-2)$

3. $4x^2 + 20x + 25$

M: 100
A: 20

$(4x+10)(4x+10)$

$(2x+5)(2x+5)$

4. A rectangular fountain in the center of a shopping mall has an area of $(4x^2 + 12x + 9)$ ft². The dimensions of the fountain are of the form $cx + d$, where c and d are whole numbers.

a. Factor to find the expressions for the length and width of the fountain.

$4x^2 + 12x + 9$

$\left(\frac{4x+6}{2}\right)\left(\frac{4x+6}{2}\right) = \overset{L}{(2x+3)}\overset{W}{(2x+3)}$

M: $3b$
A: 12

b. Find an expression for the perimeter of the fountain.

$(2x+3) + (2x+3) + (2x+3) + (2x+3) = 8x + 12$

c. Find the perimeter when $x = 2$ ft.

$8(2) + 12 = 16 + 12 = 28$

5. $x^2 - 16$

M: -16
A: 0

$(x+4)(x-4)$

6. $9b^4 - 200$

M: -1800
A: 0

~~$(3b^2-20)$~~

Can not factor

7. $1 - m^6$

M: 1
A: 0

$(1-m^3)(1+m^3)$

don't mult = -1800

$\left(\frac{9b^2-900}{9}\right)\left(\frac{9b^2+900}{9}\right)$

$(b^2-100)(b^2+100)$
nope!

Section 6 – Factor Using Any Method

Factor each polynomial completely.

1. $6t^2 + 12$
 $6(t^2 + 2)$ ← M: 2
 A: 0
 unfactorable

2. $5m^2 + 45m$
 $5m(m + 9)$

3. $5r^3 - 10r$
 $5r(r^2 - 2)$ ← M: -2
 A: 0
 unfactorable

4. $p^2 - 9$
 $(p + 3)(p - 3)$ ← M: -9
 A: 0

5. $x^2 - 25$
 $(x + 5)(x - 5)$

6. $3x^3y + x^2y^2$
 $x^2y(3x + y)$

7. $12n^3 - 48n$
 $12n(n^2 - 4)$ ← M: -4
 A: 0
 $12n(n + 2)(n - 2)$

8. $x^3 - 9x$
 $x(x^2 - 9)$ ← M: -9
 A: 0
 $x(x + 3)(x - 3)$

15. $10w^4 - 160w^2$
 $10w^2(w^2 - 16)$ ← M: -16
 A: 0
 $10w^2(w + 4)(w - 4)$

16. $3c^4 + 24c^3 + 48c^2$
 $3c^2(c^2 + 8c + 16)$ ← M: 16
 A: 8
 $3c^2(c + 4)(c + 4)$

17. $3d^2 + 13d + 4$
 $\frac{(3d + 12)}{3} \cdot \frac{(3d + 1)}{3}$ ← M: 12
 A: 13
 $(d + 4)(3d + 1)$

18. $6a^3 + 39a^2 + 45a$
 $3a(2a^2 + 13a + 15)$ ← M: 30
 A: 13
 $3a\left(\frac{2a}{2} + \frac{10}{2}\right)(2a + 3)$
 $3a(a + 5)(2a + 3)$

